

2008 JUNE

Degree - III (H), Paper - V, Group - C ¹ SUN

Date: - 22/02/2024.

Name: - Giridhar Kumar.

Topic: - The Time-Independent Schrodinger Equation: -

When the potential $V(x)$ is time-independent, we can simplify the schrodinger equation by the method of separation of variables.

$$\psi(x, t) = \phi(x) T(t) \quad \text{--- (1)}$$

Substitute into the Schrodinger Equ. ² MON

$$i\hbar \phi(x) \frac{\partial T}{\partial t} = T \tilde{H} \phi \quad \text{--- (2)}$$

Dividing both sides by ϕT , we find

$$i\hbar \frac{1}{T(t)} \cdot \frac{\partial}{\partial t} T(t) = \frac{1}{\phi(x)} \tilde{H} \phi(x) \quad \text{--- (3)}$$

Since the L.H.S depends only on t and R.H.S only on x , the only way this equ can be true is if both sides equal a constant

Say it E :

$$i\hbar \frac{1}{T(t)} \cdot \frac{\partial}{\partial t} T(t) = E$$

$$\Rightarrow \frac{1}{\phi(x)} \tilde{H} \phi(x) = E \quad \text{--- (4)}$$

July 2008	Sun	Mon	Tue	Wed	Thu	Fri	Sat
	6	7	8	9	10	11	12
	13	14	15	16	17	18	19
	20	21	22	23	24	25	26
	27	28	29	30	31		

Notes

JUNE 2008

3
TUE

Degree-III (H), paper-V, Group-C
Date:- 22/02/2024
Name:- Giridhar Kumar.

The first of these two differential eqn can be solved immediately.

$$\boxed{T(t) = e^{-iEt/\hbar}} \quad \text{--- (5)}$$

the second equation.

$$\boxed{\tilde{H}\phi = E\phi} \quad \text{--- (6) [EigenVal equation]}$$

Or more explicitly

$$\boxed{\left[-\frac{\hbar^2}{2m} \frac{d^2}{dx^2} + V(x) \right] \phi(x) = E\phi(x)} \quad \text{--- (7)}$$

4
WED

Above Equation is known as Time-Independent Schrodinger Equation.

In case of the Schrodinger equation, the constant E is called the "energy eigenvalue," and the function $\phi(x)$ is called "eigenfunction" or "energy eigenstate".

To each energy eigenvalue E there is at least one and sometimes more than one energy eigenstate, and to each eigenstate there corresponds a solution

May 2008	Sun	Mon	Tue	Wed	Thu	Fri	Sat
					1	2	3
4	5	6	7	8	9	10	
11	12	13	14	15	16	17	
18	19	20	21	22	23	24	
25	26	27	28	29	30	31	

Notes

$$\boxed{\Psi(x,t) = \phi(x)e^{-iEt/\hbar}} \quad \text{--- (8)}$$

2008

JUNE

Degree - III (H), Paper - V, Group - C

Date: - 22/02/2004.

Name: - Giridhar Kumar

Above equation are also known as stationary states. because the time the time-dependence is contained entirely in an overall phase. This means that the probability to find a particle in the neighborhood of point x , i.e

$$P_e(x) = \psi^*(x,t)\psi(x,t) e = \phi^*(x)\phi(x) e \quad (9)$$

Now the general solution to the time-dependent Schrodinger equation is,

$$\psi(x,t) = \sum_a c_a \phi_a(x) e^{-iE_a t/\hbar}$$

if the energy eigenvalue are a discrete set, then

$$\psi(x,t) = \int da c_a \phi_a(x) e^{-iE_a t/\hbar}$$

if the energy eigenvalue span a continuous range, or a combination.

$$\psi(x,t) = \sum_a c_a \phi_a(x) e^{-iE_a t/\hbar} + \int da c_a \phi_a(x) e^{-iE_a t/\hbar} \quad (11)$$

Notes

July 2008	Sun	Mon	Tue	Wed	Thu	Fri	Sat
			1	2	3	4	5
6	7	8	9	10	11	12	13
14	15	16	17	18	19	20	21
22	23	24	25	26	27	28	29
30	31						