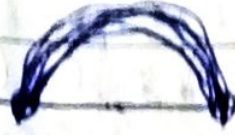


→ $\langle 1, 2, 1, 2, 1, 2, 1, 2, \dots \rangle$

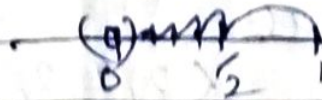


infinite many subseq can be

limit point = $\{1, 2\}$

∴ limit does not exist

→ $\langle \frac{1}{n} \rangle = \langle 1, \frac{1}{2}, \frac{1}{3}, \dots \rangle$



limit point = $\{0\}$

limit = $\{0\}$

Ex-2 Divergent sequence:

Let $\{a_n\}$ be a real sequence and
if $\lim_{n \rightarrow \infty} a_n = \infty$ or $-\infty$

then the sequence $\{a_n\}$ is called divergent sequence.

OR,

let K (however large) and

if $\lim_{n \rightarrow \infty} a_n > K$ for n then

$\{a_n\}$ is called divergent sequence.

Ex(1) $\langle n \rangle = \langle 1, 2, 3, 4, 5, 6, 7, \dots \rangle$



∴ $\{a_n\}$ is divergent

* Oscillating Sequence:

suppose $\langle (-1)^n 5 \rangle = \{ -5, 5, -5, 5, -5, \dots \}$



limit point = $\{ -5, 5 \}$ set is not

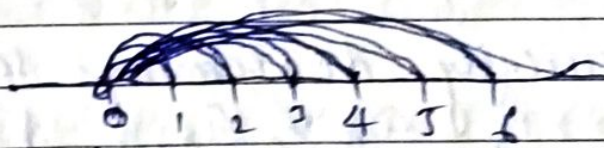
single point. The sequence converges not to a single point. The sequence oscillates.

A sequence can behave in three ways:

- ① Convergent
- ② Divergent
- ③ Oscillate.

Note that the sequence $\langle (-1)^n 5 \rangle$ has no. of elements infinite but it oscillates at 2 pts between two finite numbers of odd no. terms. Such a sequence is called an oscillating sequence.

* Let $\{ 0, 1, 0, 2, 0, 3, 0, 4, 0, 5, 0, 6, \dots \}$ be a sequence



This sequence is oscillating.

limit point = $\{ 0 \}$ but not

odd sequence \Rightarrow this is infinite oscillating seqⁿ

* Let $\langle (-1)^n n \rangle = \{ -1, 2, -3, 4, -5, 6, -7, 8, \dots \}$



C, D, O Intuitively. (.. not odd)