

Illustrations

1. Let $S = \{1, 3, 5\}$; $T = \{2, 3, 4, 5, 7\}$
 then $S \cup T = \{1, 2, 3, 4, 5, 7\}$ and
 $S \cap T = \{3, 5\}$.

2. Let $E = \{\dots, -6, -4, -2, 0, 2, 4, 6, \dots\}$
 $O = \{\dots, -5, -3, -1, 1, 3, 5, \dots\}$

then $E \cup O = \mathbb{I}$ (Set of Integers).

and $E \cap O = \{\} = \phi$

thus, E and O are disjoint sets.

Note:- It will help to remember the following results:

$$x \in S \cup T \Rightarrow x \in S \text{ or } x \in T.$$

$$x \in S \cap T \Rightarrow x \in S \text{ \& } x \in T$$

$$x \notin S \cup T \Rightarrow x \notin S \text{ \& } x \notin T.$$

$$x \notin S \cap T \Rightarrow x \notin S \text{ or } x \notin T$$

* Def (5): A non-empty set Δ is said to be an index set for the family $\mathcal{J} = \{S_\lambda\}$ of sets if for each $\lambda \in \Delta$, $\exists$ a set S_λ in the family $\mathcal{J}$.

for example; $N = \{1, 2, 3, 4, \dots\}$ is an index set for the family of sets $\{S_1, S_2, S_3, S_4, \dots\}$.

Consider an arbitrary family of sets $\{S_\lambda : \lambda \in \Delta\}$; Δ is any index set:

* Def (7): The union of the sets $\{S_\lambda\}$ is defined as

$$\bigcup_{\lambda \in \Delta} S_\lambda = \{x : x \in S_\lambda \text{ for some } \lambda \in \Delta\}$$