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Symmetric tensor \rightarrow : A tensor T_{i_1, i_2, \dots, i_r} symmetric with respect to indices i_k and i_l if $T_{\dots i_k \dots i_l \dots} = T_{\dots i_l \dots i_k \dots}$. For a second rank tensor T_{ij} , this simplifies to $T_{ij} = T_{ji}$.

A symmetric tensor is tensor that remains invariant when any pair of its indices are interchanged ($T_{ij} = T_{ji}$ for a second rank tensor). They are fundamental in physics for representing physical properties that are independent of coordinate ordering such as the stress tensor, strain tensor, momentum of inertia etc. A symmetric 2nd-rank tensor in 3D has only 6 (six) distinct components (3 diagonal and 3 off diagonal) rather than 9 (nine) reducing complexity. Any 2nd-rank tensor can be decomposed into symmetric (S_{ij}) and anti-symmetric (A_{ij}) parts. As

$$T_{ij} = \frac{1}{2} (T_{ij} + T_{ji}) + \frac{1}{2} (T_{ij} - T_{ji})$$

The sum of two symmetric tensor is symmetric. The ~~linear~~ inner product of a symmetric tensor with an anti-symmetric tensor is zero.

crucial for reducing the independent components in physical systems. Making calculations in stress, strain and relativity more efficient. Example of symmetric tensor —

Stress tensor (σ_{ij}) describe internal forces in a continuum. Inertia tensor (I_{ij}) is relates angular momentum to angular velocity. Metric tensor is fundamental in general relativity.
