

Date  
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MJC - PHYSICS, P...  
Sem - IV, Unit - 01

Spherical coordinates →  
Spherical and cylindrical coordinates are two generalizations of polar coordinates to three dimensions. For a point  $(x, y, z)$  in three dimensional space, the spherical coordinates are defined as follows.

$\rho$  → the length of the ray from the origin to the point.

$\theta$  - The angle between the positive  $x$ -axis and the ray from the origin to the point  $(x, y, 0)$

$\phi$  - the angle between the positive  $z$ -axis and the ray from the origin to the point of interest.

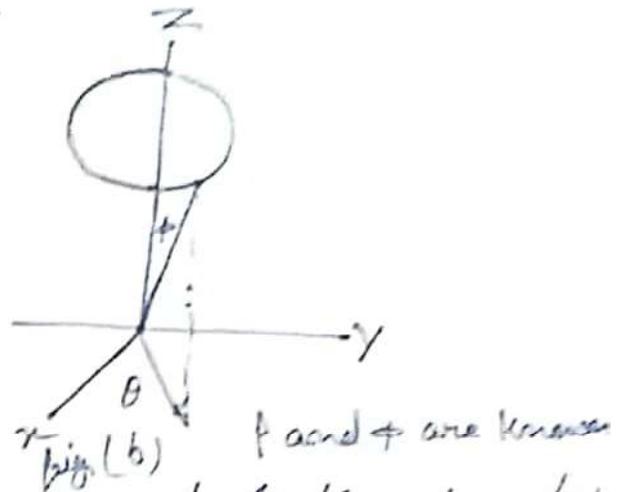
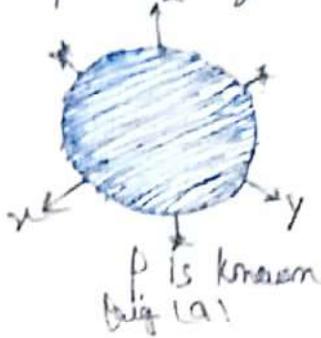
The spherical coordinates are determined by  $(\rho, \phi, \theta)$ . The relation between these and the cartesian coordinate  $(x, y, z)$  for a point are as follows.

$$x = \rho \sin(\phi) \cos(\theta), \phi \in [0, \pi]$$

$$y = \rho \sin(\phi) \sin(\theta), \theta \in [0, 2\pi]$$

$$z = \rho \cos \phi, \rho \geq 0$$

By picture (a), the first illustrates the surface where  $\rho$  is known, which is a sphere of radius  $\rho$ .



By picture (b) corresponds to knowing both  $\rho$  and  $\phi$ , which results in a circle about the  $z$ -axis. Suppose the fig (a) demonstrates a graph of ~~the~~ the earth. Then the circle in the fig (b) would correspond to a particular latitude. Giving the third coordinate,  $\theta$  completely specifies the point of interest. This is demonstrated in the following fig. If the latitude corresponds to  $\phi$ , then ~~we say that~~  $\theta$  as the longitude.  $\rho, \phi$  and  $\theta$  are known.