

Cylindrical coordinates.

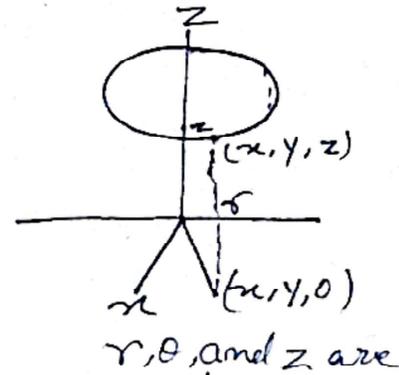
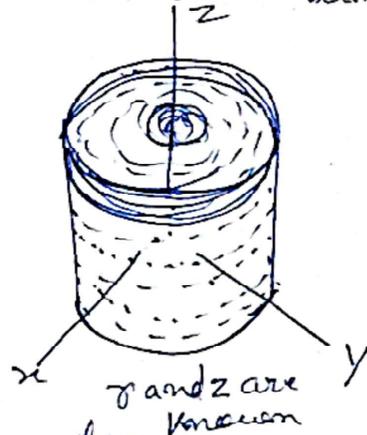
Cylindrical coordinates \rightarrow :

Cylindrical and spherical coordinates are two generalizations of polar coordinates to three dimensions. When moving from 2D polar coordinates in two dimensions, we use the polar coordinates in the xy plane and add a z coordinate. For this reason, we use the notation (r, θ, z) to express cylindrical coordinates. The relationship between cartesian coordinates (x, y, z) and cylindrical coordinates (r, θ, z) is given

$$\begin{aligned} \text{by } x &= r \cos(\theta) \\ y &= r \sin(\theta) \\ z &= z \end{aligned}$$

Where $r \geq 0$, $\theta \in [0, 2\pi]$ and z is simply the cartesian coordinate. Notice that x and y are defined as the usual polar coordinates in the $x-y$ plane. That r is defined as the length of the ray from the origin to the point $(x, y, 0)$, where θ is the angle

between the positive x -axis and this same ray
 Consider the fig. r and z are known. The cylinder
 corresponds to a given value for r . Here r is as the distance between
 a point in three dimensions and the z -
 z -axis.



Every point on the cylinder shown is at
 the same distance from the z -axis. Giving
 a value for z results in a
 horizontal circle, or cross section of the cyli-
 nder at the given height on the z -axis.
 Every point of three dimensional space
 other than the z -axis has unique cylindrical
 coordinates of course there are
 infinitely many cylindrical coordinates for
 the origin and for the z -axis. Any θ we'll
 work is $r=0$ and z is given.